An augmented canonical gravity wave

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Abstract. We add trial monopole interactions to the Schwarzschild and Reissner-Nordström metrics, carried by a massless particle which is a wave in the metric. We assume that any change in the mass and charge of the black holes must be exactly compensated by that of the waves in metric. The action was analyzed using Wolfram Mathematica and exact expressions, without numerics or arbitrary precision numbers. We find that the Schwarzschild and Reissner-Nordström solutions are degenerate as global vacuum solutions in every linear combination of these radiating wave components. Both solution families are examples where $\int_V R\sqrt{-g}\,dV = 0$ while $R_{\mu\nu} \neq 0$, such that the action of general relativity is globally minimized, but not locally vanishing. Simulation of special relativity with accelerated frames provides further evidence that general relativity requires gravitational monopole interaction. These solutions imply charged and uncharged graviton scalar monopole terms, mediated by entangled graviton groups with cancelling spin acting as composite scalars. The implied charged gravitons, though exotic, should be confined til slightly below Planck scale and typically have negligible electromagnetic effect. We develop general experimental considerations for a simple experimental test, to produce charged graviton pairs from four coincident spin-aligned photons, from a tuned laser and a nucleus. We develop cosmological considerations for the mass monopole waves, partly in order to discuss their compatibility with existing astrophysical data.

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1. Introduction

Applying the canonical quantum theory to the canonical modern theory of gravity exactly, with no or few new axioms, is regarded as extremely difficult. Nonrenormalizability of the canonical gravitational field precludes a useful or accurate physical description. “Canonical quantum gravity” proper follows the Hamiltonian formulation of mechanics. It was established decades ago [5][15], and Hamiltonian approaches based on this early work are still actively researched today [34]. Feynman path integrals and the Hamilton-Jacobi mechanics applied to general relativity have also led to foundational results [20]. The minisuperspace approximation scheme has lead to important canonical results in quantizing black holes, despite the difficulties with quantizing the gravitational field directly[6]. However, “the quantum theory of gravity,” in terms of a field or particle description, is perceived as incomplete or unsatisfactory.

Experiment confirms general relativity’s predictions of redshift and deflection of light by mass [39], and the existence of gravitational waves [1]. While general relativity and gravitational waves have general experimental support, difficulties with directly quantizing the canonical gravitational field are often taken as motivation to modify quantum or general relativistic theory [9] [25] [34]. However, there is broad consistency between prediction and experiment in application of both these theories to all phenomena but each other.

“Supersymmetry” [40] is probably the most popular axiom chosen to add to the theories of general relativity and quantum mechanics, to help alleviate their apparent inconsistency or ambiguity. It might be preferable if a quantum treatment of the gravitational field could be given with *no* additional axioms, beyond Einstein equivalence principle, the Born rule, and the other minimum required axioms of relativistic and quantum mechanics in their most canonical forms. In this paper, the author attempts quantization without “new physics” by relying on the local conservation of the stress-energy-momentum in general relativity when added to that of an apprORpiate “pseudotensor,” as due to Landau and Lifshitz [24]. Perhaps primarily due to their lack of independence as tensors, it is debated whether such gravitational pseudotensors are physically vacuous, but their continuity can be shown as a theorem of the Einstein field equations. Relying on the existence of this continuity, which is implicitly proven in past constructions of gravitational pseudotensrs, we find new modes of gravitational radiation from black holes, when we assume that local conservation is enforced between the stress-energy-momentum tensor and its gravitational complement constructed entirely from the metric and its derivatives. These newly discovered modes appear to be mass monopole and, potentially, charge monopole modes.

Gravity waves coupled to the mass quadrupole have been detected and undoubtedly exist. We expect all single gravitons to carry 2 units of spin. Like the electromagnetic force, higher pole interaction terms should contribute, which happen to correspond with overall spin values in groups of bosons entangled together by stimulated emission. If multipole interaction terms correspond to total spin values of entangled groups due to stimulated emission, we don’t expect monopole interaction terms for either the spin 1 photon or spin 2 graviton. However, either particle might be able to mediate a monopole interaction term if it is physically possible to produce entangled spin-anti-aligned groups, with 0 overall spin.

The quantum mechanical likelihood of this gravitational interaction should be determinable from how far its Einstein-Hilbert action deviates from classical solutions. However, any modification to the mathematical form of gravity waves must be able to explain observed modes of gravitational oscillation to date. In the following treatment, we will develop evidence for the existence of entagled spin-anti-aligned scalar graviton groupings mediating a gravitational monopole interaction, as well as evidence for their production by black holes, by presenting global vacuum black hole solutions to the Einstein field equations with a monopole interaction, showing the theoretical economy that follows from such solutions and discussing the agreement of this model with existing observational data. By allowing entangled spin-anti-aligned graviton groupings, carrying 0 total spin and mediating a monopole interaction, somewhat similar to photons produced in stimulated emission, we might avoid modifying both the most bedrock principles of general relativity and quantum mechanics, to address the obvious physical intractabilities of quantum gravity. By restricting to real, rather than virtual, gravitons, we hope to avoid nonrenormalizability in a limited treatment of the quantum gravitational field.

2. Method

2.1. Theory

The Euler-Lagrange equation selects the minima or extrema of the corresponding action, according to the principle of least action. The Einstein field equations are the solution of the Euler-Lagrange tensor equation for the Einstein-Hilbert action. The action depends only on the curvature for a vacuum solution:

$$S(n,m) = \int_{t_n}^{t_m} \int_V \frac{1}{16\pi G_N} R\sqrt{-g}\, d^3x\, dt, \tag{1}$$

[17], where R is the Ricci scalar, $\sqrt{-g}$ is the volume element, and G_N is Newton's constant. For non-vacuum solutions, a Lagrangian density for any non-gravitational matter fields is added to the integrand. The Einstein field equations are produced by solving the Euler-Lagrange equations or, equivalently, extremizing the action.

The volume integral is usually taken over the entire space, if possible. The boundary conditions of the Einstein-Hilbert action must be accounted to give a meaningful mechanical description via the principle of least action. Consider the variation of the Einstein-Hilbert action:

$$\delta A_{EH} = \int_V d^4x\sqrt{-g}\left(G_{\mu\nu}\delta g^{\mu\nu}\right) + \int_V d^4x\sqrt{-g}\nabla_\epsilon\left(g^{\mu\nu}\delta\Gamma^{\epsilon}{}_{\mu\nu} - g^{\epsilon\eta}\delta\Gamma^{\mu}{}_{\mu\eta}\right) \tag{2}$$

where $G_{\mu\nu}$ is the inverse Einstein tensor, $\Gamma^{\epsilon}{}_{\mu\nu}$ are the Christoffel symbols, $g^{\mu\nu}$ is the inverse of the metric tensor, and g is the metric tensor trace [30]. Over a finite volume, we must include the value at its boundary. Some research suggests this boundary and its interior bulk are holographically dual [29]. Rewritten from equation 2, this term is

$$\delta A_{boundary} = \int_v d^3x\sqrt{h}\left(Kh^{ij} - K^{ij}\right)\delta h^{ij}, \tag{3}$$

where h^{ij} is the inverse induced 3-space metric, h is its trace, and K^{ij} is the inverse extrinsic curvature [30].

The Feynman path integral formulation of quantum mechanics is a Hamilton-Jacobi approach that allows us to quantize by assigning phases to mechanical paths by their classical actions:

$$\int d\vec{x}_{N-1} \int d\vec{x}_{N-2} ... \int d\vec{x}_2 \prod_{n=2}^{N} \exp\left(\frac{iS(n, n-1)}{\hbar}\right) \tag{4}$$

is a solution to the Schrödinger equation (for a nonrelativistic action) in the limit where the time step goes to zero, where $\int d\,\vec{x_n}$ usually represents an integral over the position basis at time step n [35]. We can think of this position basis integral as rather an integral over a general configuration basis over all space at a time step.

From equation 4, virtually any arbitrary variation in the action appears to have quantum mechanical meaning and quantifiable probability. However, adding any arbitrary hypothetical charge, wave interaction, negative energy, or similar supposition to the action might lead to a description of a system which does not have a corresponding physical principle to mediate it, like many argue for an exact solution due to Alcubierre [4] that appears to rely on absolute negative energy. For example, in the action of the Schwarzschild solution, we should be able to arbitrarily vary the apparent Schwarzschild radius locally, but this implies a gravitational scalar field coupling to the mass monopole, while the hypothetical graviton is likely rank 2. The stress-energy-momentum carried away should be exactly that of an apprōrpriately chosen, locally-conserving pseudotensor, built entirely from the metric and its derivatives. Taking a time coordinate t' that is retarded by the speed of gravity or light,

$$r_s \to \mathscr{r}_s = r_s + \mathscr{r}_g = r_s(t') + 2\int_0^{r_s/2} b(k, t') \sin{(kt')}\, dk \tag{5}$$

such a quantum mechanical monopole variation is physical if a mediator scalar particle exists, where $b(k, t')$ is a general, arbitrary wave amplitude function, made proportional to the energy of the black hole. For such a particle to exist, contributing only to the Ricci scalar and not the matter field Lagrangian, it must be a composite particle of gravitons. Reports of similar monopole generalizations of general relativity, with a quantization condition, already exist in the literature [14].

To extend to the Reissner-Nordström metric, we add an analagous variation in the charge monopole:

$$q \to \mathscr{q} = q + \mathscr{q}_g = q(t') + \int_0^{q} a(k, t') \sin{(kt')}\, dk. \tag{6}$$

Our analysis was restricted to Reissner-Nordström with an exactly extremal ratio of charge to mass, at the limit of a Cauchy horizon at the same radius as the Schwarzschild horizon. No specific restraint on charge-to-mass ratio of gravitons might be required, though the author analyzed the case of emitted gravitons that maintain the exactly extremal limit, for simplicity in proof of concept.

No gravitational effect in general relativity can propagate faster than the speed of light [11]. Starting from a variation of the local apparent Schwarzschild radius, we assume that the underlying quantum mechanical basis waves travel at the speed of light. These waves should therefore also carry the energy of a massless particle away from the black hole:

$$\frac{dM}{dt'} = \int_0^\infty \hbar k \frac{\partial b(k,t')}{\partial t'}\, dk, \tag{7}$$

where M is the mass of the black hole. This constrains the parameterization of r_s:

$$\frac{dr_s}{dt'} = -2G_N \frac{dE}{dt'}. \tag{8}$$

The underlying particles must be emitted in a way that also preserves momentum, such as pairwise emission of equal energy particles in opposite directions. The underlying fundamental particles should also carry 2 units of spin, but it might be possible to emit even numbers of entangled gravitons with cancelling overall spin.

Suppressing explicit parameters, the modified Schwarzschild metric is simple:

$$g_{tt} = -\left(1 - \frac{r_s(t')}{r}\right) + \frac{2\int_0^{r_s/2} b(k,t')\sin\left(kt'\right) dk}{r}, \tag{9}$$

$$g_{rr} = \left(\left(1 - \frac{r_s(t')}{r}\right) - \frac{2\int_0^{r_s/2} b(k,t')\sin\left(kt'\right) dk}{r}\right)^{-1}, \tag{10}$$

$$g_{\theta\theta} = r^2, \tag{11}$$

$$g_{\phi\phi} = r^2\sin^2(\theta), \tag{12}$$

and all off-diagonal terms are zero. $r_s(t')$ is a parameterization such that $r_s(t')$ must take a constant value on a t' hypersurface. Additionally, the time dependence of the average Schwarzschild radius is assumed to be constrained so the energy difference implied by the change of the average radius is exactly the energy carried by the wave amplitudes according to their de Broglie wavelength. As such,

$$\frac{dr_s(t')}{dt'} = -2\int_0^{r_s/2} b(k,t')\, dk \tag{13}$$

and

$$\frac{d^2 r_s(t')}{dt'^2} = -2\int_0^{r_s/2} \frac{db(k,t')}{dt'}\, dk. \tag{14}$$

We will test whether this is a functional minimization of the action. We simply assume here that, if energy *can* be lost from the black hole, a continuity equation can be derived when the gravitational pseudotensor, constructed from the metric and its derivatives, is added to the stress-energy-momentum tensor.

These gravitational quantum variations, assumed to be carried by a discrete, massless particle, propagate along null geodesics. From the Schwarzschild line element, allowing $r_s \to \bcancel{r}_s$, we can define t' (recursively) as an exterior, outgoing retarded time coordinate which is zero on the event horizon at $t = 0$. The coordinates are more easily defined implicitly via the inverse coordinate transformation:

$$t = \frac{1}{2}\left[t' + r' + W\left(\frac{1}{e}\right)\right], \tag{15}$$

where W is the Lambert-W function, and

$$r = \not{r}_s(t')\left(W\left\{\frac{1}{\not{r}_s(t')}\exp\left[\frac{r'}{2\not{r}_s(t')} - \frac{t'}{2\not{r}_s(t')} - 1\right]\right\} + 1\right) - W\left(\frac{1}{e}\right) \tag{16}$$

Note that the dependence of $\not{r}_s$ on t' is an arbitrary parameterization, which is important when inverting the coordinate transformation.

Reissner-Nordström has a different pair of coordinates, which can only be inverted in terms of an uncommon, but "well-behaved" transcendental function related to the Lambert-W. By trial and error, the author has found that one should take $t' = 0$ at $r = r_s$ and $t = 0$, for natural expression. In spherical coordinates, there is a simple replacement for t:

$$t = r' - t'. \tag{17}$$

Suppressing the argument of $\not{r}_s(t')$ for brevity, r can then be defined implicitly as a solution to the equation

$$\frac{2r^2 - 2r(r' + \not{r}_s - 2t') + \not{r}_s(2r - \not{r}_s)[\log\left(2r - \not{r}_s\right) - \log\left(\not{r}_s\right)] + \not{r}_s(r' - 2t')}{2r - \not{r}_s} = 0. \tag{18}$$

With Mathematica, one can easily define a custom transcendental function which solves this equation given specific arguments, and this is sufficient to carry out our analysis.

This is enough to form our actions in coordinates that mix t and r with t' and r'. Then, we can use the Jacobian to transform coordinates and derivatives to write the action entirely in terms of t' and r'. We need to check the boundary conditions of the action for validity, in that it should vanish. We avoid all arbitrary precision numerics.

2.2. Computational simplification

All computational analysis was carried out in Wolfram Mathematica. Several notebooks demonstrating the results are available along with this paper. A publicly available differential geometry package [21] was used to form the Ricci scalar, Ricci tensor, and volume element for the Einstein-Hilbert action. The same package was used to form the extrinsic curvature tensor, the extrinsic curvature trace, and induced metric in order to check the boundary conditions. The resulting Mathematica notebook files are highly optimized and run to completion in minutes on a home computer.

The Mathematica function "*Hold*" and functional "*Inactive*" were used to reduce computational overhead. "*Hold*[*x*]" is equivalent to "*x*" when used in a Mathematica expression, but the form of its argument is "held" without evaluation. "*Inactive*[*f*]" prevents Mathematica from attempting to apply a function *f*, leaving it present with all its usual properties, but never attempting to evaluate an "*Inactive*" function.

The goal is an action entirely in terms t' and r' rather than t and r. Mathematica finds coordinate transformations between t and r, and t' and r', with the use of the "*ProductLog*" function, or Lambert W function, such that *ProductLog*$[z]$ can be defined as the solution of $z = we^w$ for w. The partial derivatives for the Jacobian were formed with this transformation. The boundary conditions were checked for both a t hypersurface and a t' hypersurface, and the boundary provides no contribution to the action. We form the Schwarzschild metric in the usual (t, r, θ, ϕ) basis, but we allow function dependence on t' and r'. Explicit dependence of t' and r' on t and r was carried through in all cases for Mathematica to recognize the need for t and r derivatives, until t and r derivatives could be substituted out of an expression. Without explicit dependence, $\frac{\partial t'}{\partial t}$ and $\frac{\partial t'}{\partial r}$ would be dropped incorrectly from expressions. Using equations 7 and 8, derivatives of $r_s(t')$ were systematically substituted for their equivalent in emitted wave amplitude. At each step, the notebooks programmatically check the partially transformed action for presence of $r_s(t')$ derivatives. After each step these derivatives are found, they are immediately removed by this same substitution. Before the explicit dependence of "$t'(t, r)$' and "$r'(t, r)$"' on t and r is removed, it is programmatically checked that the expression contains no derivatives of t' or r'. The explicit dependence is then removed, and t r are directly substituted out entirely in terms of t' and r'.

Mathematica is not directly capable of solving for a closed form for t' and r' derivatives with an exact definition of these coordinates, with "*Solve*[...]" or "*Reduce*[...]". The author's approach was to replace dependence on $\mathscr{r}_s(t')$ with dependence on $r_s(t')$ in the definitions of t' and r'. This approximation should reproduce the average behavior over full gravity wave wavelengths, since the average monopole contribution over full wavelengths is zero, since it is the average over full sinusoidal waves. It was checked that the boundary conditions give zero contribution for either the exact definition or our approximation. However, we are self-consistently restricted to integration over full monopole term wavelengths, after this approximation.

The expression is then out of mixed coordinates, but unsimplified and extremely unwieldy. Direct simplification by built-in Mathematica functions takes an extremely long time. Hence, linear superposed wave components are entered as test forms for $b(k, t')$. "*Dispatch*" was used to substitute function arguments to help simplify the expression with good computational performance. Up to this point in the program, no numerical functions or arbitrary precision math is used, using effectively "lossless" Mathematica operations. This relies entirely on exact numbers and symbols, by Mathematica's standard of exact numbers, and does not suffer from loss of precision due to "machine epsilon" or float rounding.

2.3. Special relativity in accelerated frames

Additionally, qualitative simulation of canonical special relativity in time-varying accelerated frames was carried out in a flat background. Source code came from the OpenRelativity project by the MIT Game Lab [23], as well as the author's own modifications to handle accelerated frames and Einstein equivalence principle. The OpenRelativity project is written in and operates in the Unity video game engine.

The author obtained a copy of the base OpenRelativity project via its open source repository on Github. The author has no affiliation with or endorsement by the creators and maintainers of the original project, though it was generally made available for use and modification by them under the (open source) MIT License. The MIT license applies both to the original project as well as modifications to the software by the author. The license disclaims '... THE SOFTWARE IS PROVIDED "AS IS", WITHOUT WARRANTY OF ANY KIND, EXPRESS OR IMPLIED, INCLUDING BUT NOT LIMITED TO THE WARRANTIES OF MERCHANTABILITY, FITNESS FOR A PARTICULAR PURPOSE AND NONINFRINGEMENT...'. The full text of the license is available at https://opensource.org/licenses/MIT. The author interprets that those responsible for the original project do not warranty this software for any purpose, and the author does not warranty his modifications to the software for any purpose. However, the author has made potentially instructive modifications to the original code, which might be of interest or use, with proper oversight and with or without further modification.

The part of heuristic interest for this paper relates to a relatively small segment of code in a modified "shader" program. The intent of this part of the author's modificatian to the code is to approximate special relativity in a first-person accelerated frame of reference, by proceeding in several steps:

(i) Starting in a common "world frame," or "lab frame," we Lorentz boost to a first-person rest frame.
(ii) In the first-person rest frame, we calculate the metric under the effects of first-person acceleration, as per Rindler and common pedagogical treatment of accelerated frames in special relativity[18][33].
(iii) We update objects' time and spatial coordinates based on speed of light delay from the first-person position, based on the calculated metric.
(iv) We Lorentz boost from the first-person rest frame back to the common "world frame," or "lab frame."
(v) The underlying engine's update loop proceeds to repeat this process over time, as a finite difference time-step.

If waves arise in the metric due to these steps, we can assess their form and nature. The simplicity of this method makes it easier to investigate and independently reproduce than the different analysis described above, of black hole metrics, carried out with Wolfram Mathematica.

The author's modified version of the code has been made available under the MIT License at https://github.com/WrathfulSpatula/OpenRelativity.

3. Results

3.1. Analysis of black hole metrics

Analysis with Mathematica shows that every linear combination of variation wave components has exactly 0 global Einstein-Hilbert and is therefore a functional minimization of the action of the general relativity and solution to the Einstein field equations. The boundary term of the action also vanishes. 0 volumetric Einstein-Hilbert and 0 boundary terms result for any volume that encompasses all gravitational radiation from the black hole, assuming the time-dependent radiation is "turned on" on at a certain point. (Remember that our motivation was to find the degree to which the monopole interactions deviate from the path of least action. Also, remember that our test variation is not fully general and arbitrary at this point, such that we do not mean that a perfectly arbitrary variation always produces a solution.)

If the metrics are truly vacuum solutions, we expect their Ricci tensor to vanish in all components. Forming the Ricci tensor in Mathematica for the modified Schwarzschild metric in the same way as the global Einstein-Hilbert action, we find that all terms except the "t-t" or "0-0" component of the Ricci tensor vanish. Intuitively, the spatial volume of 4-dimensional test balls are preserved, but the passage of time in their interior is deformed relative to flat space. The limit of this component of the Ricci tensor approaches 0 as $t' \to r'$, which is true for all exterior radially-outgoing light-like paths. When the time interval deformation is integrated globally, there is 0 average deviation from vacuum, since the global action is 0. These solutions are globally equivalent to vacuum on average, and therefore functionally minimize the action of general relativity, but these are not locally equivalent to vacuum; they contain real gravitational radiation.

For the Reissner-Nordström modification, the action is again globally equivalent to vacuum, but the Ricci tensor does not completely locally vanish. At least all off-diagonal terms of this metric's Ricci tensor vanish. Due to reliance on the Lambert W-like special function described in the methods section, intermediate outputs of this function are returned for all diagonal terms of the Ricci tensor, which might or might not ultimately be shown to vanish. However, integrating the Ricci scalar globally, Mathematica again shows that the average global curvature vanishes identically, such that these metrics satisfy the action principle of general relativity.

Waves emitted by a Schwarzschild black hole carry net mass away from the black hole, while waves emitted by an extremal Reissner-Nordström black hole carry energy and charge. Waves coupling to angular momentum are presumably the canonically established modes of the theory of gravity waves, carried by a (free) spin 2 graviton. Extending the treatment to a more general subset of a (Lorentz boosted) Kerr-Newman solution is computationally challenging, but we can develop particle mechanics and thermodynamic consideration based on the assumption that this generalization exists, to start to reconcile this hypothesis with existing observational and experimental data.

3.2. Analysis of special relativity with accelerated frames

Wave-like phenomena in the metric are clearly visually discernible in the author's modifications to OpenRelativity, under changing first-person acceleration. This becomes apparent per the steps outlined in the methods section. Waves appear at approximately right angles to the direction of first-person perspective acceleration. (A demo of the results is available in a publicly available fork of the project, by the author.)

4. Discussion

4.1. General considerations

The reader might think that, if our motivation is Feynman path integral quantization, our variation should be entirely general and not restricted to these scalar waves. We stress that our analysis shows that these metrics all have exact global vacuum action, when self consistent amplitudes and wavelengths are chosen. They are therefore (degenerate) exact vacuum solutions to the classical Einstein field equations, as valid as Schwarzschild prior to explicit quantization. We are motivated to test these metrics as solutions to the Einstein field equations by assuming the existence of a pseudotensor continuity equation that implies an underlying discrete, massless, gravitational force carrier particle. At this point, we can completely dispense with Feynman path integrals and any form of explicit quantization for the composite system, if we wish, while still assuming the existence of an underlying discrete force carrier. However, these solutions' degeneracy is easily interpreted in terms of energy degenerate quantum eigenstates, assuming generalizability of our treatment to a Lorentz boosted Kerr-Newman metric. We might not as easily interpret this degeneracy in the Einstein field equations without knowledge of the resulting trivial Feynman path integral. We liken our solutions to Alcubierre's, because they are either physically realized, barred by the requirement of an exotic, nonphysical particle, (in this case, a composite graviton scalar,) or else fundamentally theoretically problematic for general relativity due to their degeneracy with the Schwarzschild solution. We submit an explicit derivation alongside this paper, in the form of Mathematica notebooks, and eagerly invite criticism of the method.

Note that all that follows depends simply on the existence of solutions for such massless, discrete, vacuum, scalar gravitational waves. Almost nothing we are about to develop depends on any other particular aspect of the solutions' form, except that solutions exist for black hole metrics with linearly superposable, vacuum, scalar monopole radiation that couples to all conserved quantities, as we assert that our proposed solutions are for mass and charge. We offer our computational derivations as explicit, rigorous, and faithful, but we appreciate that this could be difficult to confirm; the exact solutions' forms do not matter to what follows.

4.2. Analysis of special relativity in accelerated frames

The wave phenomena observed in special relativistic accelerated frames can be interpreted via Einstein equivalence principle and Gaussian surfaces.

By Einstein equivalence principle, first-person acceleration is locally indistinguishable from a gravitational field. An equivalent stress-energy-momentum configuration to first-person acceleration in a flat background could be a two dimensional "sheet" of particular mass density, extending infinitely in all directions at right angles to the direction of first-person acceleration. The distance between the first-person perspective point and the "sheet" of mass does not matter, by argument from Gaussian surfaces. A change in magnitude of first-person acceleration is then equivalent to a change in mass density of the "sheet" at an earlier time. At the exact idealized first-person position, no gravitational waves are observed. This point, (or an arbitrarily small neighborhood around it, by requirement of local flatness,) is the only region in which both Einstein equivalence principle and Birkhoff's theorem strictly apply. We see gravitational wave phenomena as we move out from this region. The further out we move from this region of exact symmetry, the more pronounced the wave phenomena become. These waves must be monopole in nature, as our equivalent mass configuration per Einstein equivalence principle acts as a mass monopole.

We see here, as in our modification of Schwarzschild, that Birkhoff's theorem relies on symmetry and is not necessarily stable. Further, we see that a treatment as limited as special relativity in reference frames with time-varying acceleration requires monopole radiation, though we do not necessarily interpret these waves in the metric as gravity without Einstein equivalence principle and the Einstein field equations.

4.3. Particle mechanics

Birkhoff's theorem implies that a stationary, static black hole cannot emit gravity waves. Common derivations of Birkhoff's theorem assume a *locally* identically vanishing Ricci tensor [12], which is sufficient, but not necessary, for the global Ricci scalar to integrate to 0 and therefore functionally minimize the action of general relativity. We have two such solutions in hand, represented in this paper, for which $\int_V R\sqrt{-g}\,dV = 0$, while $R_{\mu\nu} \neq 0$, and this is the specific assumption on which Birkhoff's theorem fails to speak against the existence of these solutions. For these minima of the action, the Ricci scalar integrated globally or over a "large enough" region vanishes identically, specifically when the limits of integration do not have a boundary "in the middle of a gravity wave," while R_{tt} only vanishes on light-like paths. (All other components of the Ricci tensor vanish identically in general.)

There is precedent in the literature for reasonable hypothetical counterexample against a specific intermediate argument of Birkhoff's theorem, that a spherically symmetric vacuum solution must have a time-independent metric. Tryon specifically stated that his proposal of "vacuum genesis," of the universe arising as a vacuum fluctuation from a null observable state, requires that the universe keeps the overall quantum numbers of the vacuum, therefore requiring homogeneity and isotropy [38]. This implies a spherically symmetric, time-dependent metric, which would be a counterexample to an intermediate step upon which Birkhoff's theorem relies, in common textbook derivations. If such a solution requires a minimal quantum deviation from perfect spherical symmetry, it seems to require only a tiny deviation from it at most, suggesting that this spherical symmetry requirement of Birkhoff's theorem, leading to time-independence, might be ruined by even deviations from spherical symmetry due only to uncertainty principle. To physicists' intuition, if Birkhoff's theorem were to actually rely intermediately on specifically perfect symmetry, it is likely to be an effectively trivial result of little physical significance, due to the general instability of perfect symmetry in practice in physical reality [36].

Our augmented wave approximately obeys a law analagous to Gauss' Law,

$$\Phi_G = \frac{M(t')}{4\pi G}\left(1 + \int_0^{\frac{M(t')}{2\pi}} b(k,t')\sin(kt')\,dk\right) = \oiint_S \boldsymbol{G}\cdot d\boldsymbol{A}, \tag{19}$$

where the wave term is quantum mechanically equiprobable in all energy-conserving b.

A modified Schwarzschild solution with a mass monopole interaction term implies a scalar particle, while there is excellent evidence to suggest that the fundamental graviton carries two units of spin, implying a quadrupole interaction. However, the fundamental photon carries one unit of spin under all cases, implying a dipole interaction, while it is uncontroversial and well known that the electromagnetic interaction has a quadrupole term and and higher order terms. Before we deal with gravity, how does a particle with one unit of spin mediate a quadrupole interaction, implying two units of spin?

In stimulated emission, photons are emitted entangled and spin-aligned. Position-entangled groups of photons can carry n units of spin with n being an integer greater than or equal to 1. These available spin states correspond with exactly the dipole, quadrupole and higher order terms of the electromagnetic interaction, as if entangled, spin-aligned photons act as composite mediators of higher order interaction terms. We'd probably expect the same behavior from gravitons produced by stimulated emission, carrying $2n$ units of spin, with n being an integer greater than or equal to 1, allowing the gravitational interaction to mediate interactions of higher pole number. A scalar interaction might surprise us, implying an entangled spin-anti-aligned state. With valid monopole interaction solutions in hand, though, they are easily explained by exactly this configuration, of entangled spin-anti-aligned gravitons. We will further show that such a gravitational monopole interaction has a great theoretical economy and agrees with existing observational data, supporting the validity of our proposed solutions.

Our modified Reissner-Nordström solution motivates charged gravitons. We admit that this is exotic, and it might be physically barred for other reasons despite the author's assertion of the existence of a such a solution to the Einstein field equations, as stated earlier. So long as it follows that gravity's typical direct interaction with electromagnetism is negligibly tiny, though, this might be an exciting prospect for carefully tuned direct experimental tests of gravity, so let us follow this line of reasoning through fully and credulously.

If a charged graviton can exist, we must consider its relevance to Penrose's cosmic censorship hypothesis [31] when the particle is emitted or absorbed by a black hole. If a beam of charge-carrying, massless particles were to impinge on a black hole with extremal charge of same sign, the requisite energy for a charged graviton approaching from infinity to overcome the electrostatic repulsion of an extremally charged black hole is exactly the energy required to keep the charge-to-mass ratio of the black hole extremal or less, otherwise electromagnetically deflecting the beam over the weaker gravitational attraction.

The analagous radiation for the Kerr metric must carry net angular momentum, from orbit or spin. While our scalar radiation should internally couple to the mass monopole in a rotating black hole, the mediating scalar must travel through the Kerr ergosphere to be emitted into the external region. Objects in the ergospere must corotate and are driven to spin opposite the spin of the black hole. If the Penrose process [32] separates entangled composite scalar components, such that part is ejected and part is reabsorbed, the ejected component carries net spin angular momentum, effectively coupling it as a spin-2 interaction to the angular momentum and kinetic energy, first reducing these quantities rather than the rest mass of the black hole past the extremal point implied by cosmic censorship. Similarly, if electromagnetic forces separate scalar multipoles made of cancelling charged particles, so that part of the multipole may exit the internal Cauchy horizon of a Reissner-Nordström black hole, charges opposite the net charge of the hole are drawn in while charges like the net charge of the hole are forced out, so the component ejected should carry nonzero charge (and zero spin, such as in the form of a magnetic quadrupole of two like charges). Both conditions apply to the Kerr-Newman metric, describing a rotating, charged black hole.

Fundamental charge values of ±1 and 0 for gravitons are implied by several considerations. Firstly, known gravity wave modes must be carried by an uncharged graviton. ±1 would allow entangled gravitons carrying a charge monopole interaction to interact with a charged lepton to produce an oppositely charged anti-lepton, if the graviton can carry other conserved quatities like lepton number, as well. (This treatment ultimately suggests to the author that the gravitational interaction is capable of carrying all conserved quantities, at least at sufficient unification scales.) A scalar carrying like charge would always or almost always be unable to overcome electrostatic repulsion to impart the charge it carries to another charged fundamental particle, while oppositely charged leptons would attract scalar charged graviton groupings. This is one of the few available hypothtetical modes of particle-mixing interaction with the Standard Model, as our treatment does not imply that these particles should carry flavor or color charges. The energy necessary to separate oppositely charged massless particles from vacuum is u^2 or α, which implies confinement of hypothetical charged gravitons.

Of course, we see no obvious experimental or observational evidence that the graviton can ever interact electromagnetically, but fully developed consideration of this hypothetical charged graviton actually implies confinement and very weak, sub-

Planck scale electromagnetic interaction. If a thermal gas of gravitons emitted from a black hole contains many positively and negatively charged gravitons, they would tend to be bound in zero net charge multipoles of small moment. (Further, if oppositely charged gravitons are antiparticles, we expect annihilation of bound pairs, but ignore this momentarily.) Our modified Reissner-Nordström solution implies that direct production of entangled, charged gravitons acting as composite scalars. Charged graviton dipoles emitted together this way would oscillate to a distance of about one Planck length at a temperature of u^2 or α, the fine structure constant (in Planck units), at which point they would be effectively freed at the scale of the gravitational interaction. This effectively confines them below extremal ratios of energy to charge, below α times the Planck energy. This is roughly on order of or higher than commonly expected grand unification energy scales for the other three fundamental forces, at about $9 \times 10^{25} eV$. To be emitted with little potential energy, with net magnetic and electric fields close to zero and with zero net spin, configurations would have to be bound in quadrupoles of two positive and two negative charges. The charges and electromagnetic fields would completely cancel in the limit of zero kinetic energy and zero graviton separation, which seems to be the absolute gravito-electromagnetic vacuum state of our field. If this is the true gravito-electromagnetic vacuum point of the field, this also suggests how nonzero charge can arise from vacuum without infinite self-energy. The oscillating multipoles radiate electromagnetically, but the momentum carried must come from the original graviton multipole. The multipole and radiation from it would travel the same direction at the speed of light, so emitted photons can be reabsorbed by the multipole, also traveling at the speed of light. This would result in oscillation between gravitational kinetic energy and electromagnetic potential energy, with little or no effective net radiation perpendicular to the path of the multipole. This picture suggests confined, effectively negligible electromagnetic gravtion interaction until distances smaller than the Planck length. Further, if these particles are emitted in scalar pairs and can annihilate, we do expect an excess of photons as a breakdown product from black holes, but we expect almost no other obvious electromagnetic interaction until past grand unification scale. (We will further discuss exactly this expected photon excess in one of the next sections.)

If the occurrence of black holes with significant net charge is rare, we expect the emission of graviton groupings with net charge to be rare, as well. It can be easily checked that if like-charge gravitons were emitted entangled with opposite spin, magnetic and gravitational attractive forces between particles at sub-Planck distance from each other would overcome electrostatic repulsion, allowing them to exist as scalar groupings.

These gravitational monopole couplings to mass and charge should be observed generally in matter. We expect the background temperature of charged gravitons to be very low, and we would not expect to observe charge monopole interactions typically in nature at the current cosmological epoch, due to the just sub-Planck scale energy required to separate massless charged bosons past Planck length. Rest mass exchange would be relatively more common. If the known masses of the Standard Model particles represent the particles' gravitational ground states, gravitational rest mass excitation might still not be typically detected in the lab, but the relatively low background temperature of scalar graviton groupings, due to black holes and cosmological artifact, could impart additional mass on astronomical scales of matter distribution. Since massive Standard Model particles acquire their masses via interaction with a scalar field with a nonzero vacuum expectation value, due to spontaneous symmetry breaking [13] [16] [19] [22], the observed fundamental masses cannot be reduced without reducing the expectation value for this field, by increasing the energy of the field. Therefore, the observed fundamental masses should be the ground states of the gravitational mass monopole interaction.

4.4. Thermodynamics

Consider only the purported mass monopole interaction, for now. Having all these equiprobable modes of breakdown available to any black hole naively implies a "particle lifetime" of r_s Planck units of time, by Fermi's golden rule, and an average loss of half its energy as gravitational radiation in the event of breakdown. (We develop this "naive" approach to show why it is probably wrong.) Most of the gravitons emitted would take on order of r_s Planck times to be emitted, implying a roughly constant thermal spectrum for astronomical black holes. The average loss of mass, before any consideration of background temperature, would be half a Planck mass per Planck time. Other conserved quantities including momentum, angular momentum, and potentially charge, should be radiated proportional to their fraction of "extremalness," with extremal black holes following a well-known constraint

$$m^2 \geq a^2 + q^2, \tag{20}$$

in the Kerr-Newman metric, with assumed Lorentz invariance, implying

$$E^2 \geq m^2 + p^2 + a^2 + q^2, \tag{21}$$

[27] with energy E, rest mass m, momentum p, angular momentum parameter a, and charge q, such that $a/(2r_s)$ units of angular momentum should be radiated in a Planck time, and so for all conserved quantities that the graviton may carry. This is independent of whether radiation can only be perpendicular to the event horizon, or if it can emit at any angle.

These "naive" breakdown considerations are probably not realistic. They imply up to half of the mass of a body like Sgr A*, millions of solar masses, being emissible in a single graviton. The de Broglie wavelength for any graviton with Planck energy or greater fits within its own Schwarzschild radius, and this is not a case we should expect to treat with Fermi's golden rule and perturbation theory without additional considerations.

Gravitons with de Broglie wavelengths that fit inside their Schwarzschild radii should be black holes with extremal or excess amounts of momentum, and therefore naked singularities. This suggests they cannot satisfy Penrose's cosmic censorship hypothesis. The emission of a black body spectrum from a black hole, as per Hawking, is expected to carry greater thermodynamic entropy than that lost from the black hole, but the emission of a single graviton heavy enough to be a black hole itself does not. If an original black hole were to break into a lighter black hole and such an extremal black hole graviton, heuristically, the event horizon area of the remnant added to the event horizon area implied by the Schwarzschild radius of the graviton is less than the area of the original black hole. Though thermal radiation adds an amount of entropy, this is offset by reduction in entropy due to to the reduction of total event horizon area [8]. It is clear that the spontaneous split of one black hole into two is not a thermodynamically favorable process, at least when all breakdown products carry about a Planck mass or greater. A more realistic approximate model assumes only thermodynamically favorable graviton emission usually happens, with an average emissive power of approximately $E_P/(2r_s)$, with "E_P" being the Planck energy. This is a correction in addition to Hawking radiation, offset by a background temperature for our waves.

In the event that a second black hole of equal mass covers some solid angle of emission of a first black hole, the net power released by the two is some amount less than this maximum power, as the two absorb a fraction of each other's emission. Bringing two test black holes closer together, the net power emitted should be gradually reduced, most obviously in the case of effective partial or total overlap between the event horizons, where emission from the interior portion of one event horizon cannot escape the other exterior horizon. Drawing two test black holes from infinitely distant to the point of total overlap of event horizons, we expect a smooth reduction of the net emission from the implied maximum power to half of the maximum value.

Charge neutral, zero spin multipoles made of charged particles are also available for mass monopole radiation, if charged gravitons exist. However, these should have high tendency to decay into photons. This could multiply the total gravitational radiance by about a factor of 5/4, assuming radiation occurs in quadrupoles of two oppositely charged particles apiece, but this extra component should be observed almost entirely as photons some short time after emission. The expected power of emission has an inverse proportionality of black hole surface area to temperature, like Hawking radiation. For an object the size of Sgr A*, the photon temperature from this mode of breakdown would be about $0.02K$. For a black hole of about 6.6 solar masses, the surface temperature would appear to be approximately $440K$ to an observer at infinity, suggesting a potentially observable infrared correction to observation of V616 Mon and small black holes in general. The wavelength peak from this temperature would be about $6.6\mu m$. Munor and Mauerhan report excesses at $4.5\mu m$ and $8\mu m$ from three quiescent low-mass black hole candidates [28]. However, the complicated binary nature of the nearest systems suspected to contain black holes might allow many reasonable and consistent spectra models, and might not be capable of providing strong proof for charged gravitons.

4.5. Cosmology and dark energy

These monopole waves should have a cosmological background temperature, which would have frozen out at the beginning of the Grand Unified Epoch and spread similar to a photon gas since that time. To agree with observation, the background temperature today need either be negligible, or else take a form whose identity is not well understood, which we posit could be "dark energy." To be confused for a true cosmological constant, the boson gas must be relatively weakly interacting, which it is, and the apparent energy density must stay close enough to effectively constant with the expansion of space. We propose this weakly interacting gas temperature could stay effectively constant with the expansion of space due to being at a critical point of a phase transition, buffered in temperature by the evaporation of primordial black holes. Further, this background temperature would impart additional mass over large ensembles of baryons, due to its nature as a gas of scalar particles coupling to the mass monopole term of gravity.

We can reconcile this hypothesis with limits imposed by observations that have already been made. Most of our estimates here depend directly on a high precision measurment of dark energy density, for which data in the literature is limited, beyond the currents limits of the Planck collaboration [2]. We take an estimate of about $7x10^{-30}g/cm^3$, a commonly quoted value for this quantity, and we estimate quantities that follow from it to the first significant digit or order of magnitude.

If dark energy were purely this scalar background, it would have a temperature of very roughly $40K$. LIGO has set a limit on the maximum amount of stochastic gravity wave background in the $10Hz$ to $100kHz$ range at not greater than 6.9×10^{-6} times the critical density of the universe, with 95% confidence [26]. The quantum mechanical distribution of energies in a masslass scalar boson gas puts our energy density in this frequency range on about the 10^{-30} scale of critical density fraction, far below LIGO's limit.

To sufficiently buffer the temperature of the gas with a phase transition, through cosmological expansion at the current epoch, the equivalent of $(3\times)10^{37}kg$ worth of black holes around one Planck mass in size must evaporate per second across the whole of the observable universe for constant energy density. If this rate of evaporation were constant throughout the age of the universe, and if the local age of the universe we observe is linearly interpolated between the Big Bang and present day, (which is an extremely rough first-order approximation, but probably representing a reasonable upper limit, due to the actual distance dependence of redshifts), it implies total mass evaporation on $(5\times)10^{51}kg$ scale compared $10^{53}kg$ scale for the estimated mass contained in the entire observable universe. This appears to be the tightest bound on our model, since it is known that light primordial black holes do not contribute a significant fraction to the present critical mass density [3] [7] [10] [37]. However, this mass need not all actually come from primordial black holes. The scalar graviton radiant power of black holes is inversely proportional to event horizon area, as with Hawking radiation. Every black hole less than very roughly 200 solar masses (probably better estimated at about 170 solar masses, in the second significant digit,) source enough radiance to more than compensate incident "dark energy" on their horizons, if it is this scalar composite graviton radiation. As space expands, the net output of every black hole smaller than this critical mass increases due to temperature difference on their horizons, like "ice in a glass of water," "melting" to contribute their latent monopole excitation to the background temperature, at a phase transition point. This could stabilize the average temperature over time and give the appearance of a constant intrinsic energy density to spatial volume. Additionally, if the present dark matter mass fraction of light primordial black holes is no greater than 2%, this alone is sufficient to maintain the apparent constancy of the dark energy background for over a billion of years into the future, by our model.

It is worth noting, as we have argued from the continuity theorem of the stress-energy-momentum when an appropriate pseudotensor is added, that this theorem should hold for photons in an FLRW universe. That is, when the stress-energy-momentum of an expanding photon gas is reduced by redshift, stress-energy-momentum continuity implies that it must be given up to the stress-energy-momentum of gravity, as gravitational waves. For an oriented "light ray" being redshifted by the expansion of space, gravitons must compensate the energy and momentum lost. The simplest compensation would seem to be made by a spin-0 "gravity ray" of the same orientation and position. This could give a very modest contribution to the gravity wave background, though it is insufficient to primarily buffer the cosmological phase transition we are considering. However, this effect becomes much more significant in the redshift of the hyperrelativistic gravity background temperature itself. The redshift of massless graviton must be compensated with the production of more gravitons, in self-coupling, sufficient to preserve local conservation of energy and momentum.

The author regrets that we lack data to provide better than an order of magnitude, rough feasibility analysis of this model for the moment. However, this analysis is qualitatively and even quantitatively insensitive to a factor of at least 10 in either direction times the estimate for dark energy, except for the required mass of light primordial black holes, which also gains or loses about a factor of 10, and except for the significant digit of the Kelvin scale temperature, which is unimportant to us here except as an intermediary quantity. Much about the usual treatments of a hypothetical scalar particle as dark energy particle or inflaton apply to the scalar presented here. In the limit of no low mass primordial black holes for a phase transition model, this particle still closely resembles other hypothetical dark energy candidate scalars, and could be expected to perform similarly. Further, this model has no tunable parameter, if the mass distribution of primordial black holes can be ascertained by observation or self-consistently fixed in simulation and if the proposed breakdown products can be shown to be a requirement from first principles. The model has the potential to explain dark energy entirely or virtually entirely, in addition to being a scalar inflaton candidate. Further, perhaps best of all, we argue that this requires no "new physics," that it results from a solution to the canonical Einstein field equations directly under only the assumption of continuity of with nongravitational plus gravitational stress-energy-momentum, with gravity mediated bya massless, discrete force carrier.

4.6. General experimental design

If charged gravitons exist, we expect pair production of dipoles under the right circumstances. Specifically, a charged graviton dipole with aligned spin should have nearly cancelling electric and magnetic fields. Four coincident, spin-aligned photons of low energy should be capable of producing a confined graviton dipole. Three aligned-spin photons could be provided by a laser, while the fourth unit of spin could be supplied by virtual exchange with a nucleus, similar to lepton pair production.

A laser with tuned gain could increase the fraction of the photon population that is coincident with the total spin of three units or greater. Since the poles of the graviton multipole are separated by less than the Planck length, creation by the interaction of photons from a laser that are not position entangled at the same point is unlikely, though one additional spin-aligned photon must be supplied from a different direction, in order to reduce overall net momentum from $E = pc$. Ideally, a laser should have its entire emitted photon population in sets of three photons entangled by stimulated emission. A scalar entangled grouping cannot be produced this way due to spin angular momentum conservation, but higher spin moment groupings should also contribute, so long as their electromagnetic fields are effectively externally screened by the Planck length.

There would be almost total electromagnetic screening, though such exactly coincident photons would couple to virtual graviton pairs with the coupling constant of elementary charge leptons. Therefore, the dipole is not likely to be directly detected, but the energy loss from its production could be. The charges would have higher tendency to separate in the presence of an eletric field directed parallel to the dipole, and perpendicular to the laser beam, such as could be applied by the presence of a nucleus, with which an additional aligned unit of spin must be exchanged. A graviton dipole could annihilate to produce photons again, as explained above. They should tend to recombine into four photons scattering with a spread of angles. Energy and momentum conserving breakdown products appear to be relatively degenerate, so photons produced by annihilation could be randomly polychromatic. The chance of collision by the fourth photon is higher at greater photon energies due to the reduced de Broglie wavelengths, though it should be possible to achieve pair production with lasers with photon energies less than the masses of lepton pairs. If massless charged gravitons exist, pair production should be possible to the limit of no exchange with a nucleus or applied field, with only four coincident spin-aligned photons, though not necessarily with great frequency.

At high energies, if electron-positron pair production cross section goes like

$$\sigma \propto Z^2 \log\left(k_0 - k_{crit}\right) \tag{22}$$

with Z being the charge of the nucleus, k_0 being the incident photon wavenumber, and k_{crit} being the critical wavenumber for electron-positron pair production, at minimum sufficient to provide the mass of two electrons, then graviton pair production should go like

$$\sigma \propto \left(\frac{Z}{2}\right)^2 \log{(k_0)}. \tag{23}$$

We assume here that the entirity of the laser is in spin triplet sets of photons, and that the spins of the charged nucleons are random. With ideal laser population statistics, high energy production of electron-positron pairs limits to a factor of 4 greater than graviton pairs. It is possible to approach a graviton cross section approximately equal to electron-positron cross section if all laser photons come in spin-aligned triplets and if charged nucleon spins are aligned with these triplets. The laser could be passed through a polarizer, and the nucleons could be magnetized. We see that, except under strictly ideal conditions, graviton pair production is significantly less than electron-positron pair production at high energies. At low energies, the photoelectric effect and Compton scattering appear to usually dominate. Below the threshold of the photoelectric effect, the impinging photon de Broglie wavelengths are large, and the chance of interaction is therefore low. In general, there might be no regime, or a very limited regime, where graviton pair production is expected to both occur at detectable levels and be the dominant mode of interaction. Detection might require a combination of careful experimental tuning and precise subtraction of these background processes.

5. Conclusion

Our scalar gravity wave augmentation leads to an infinite family of linearly superposable radiating vacuum solutions for the Reissner-Nordström and Schwarzschild metrics. If a physical particle exists that can mediate this wave, the only plausible candidate is direct emission of entangled gravitons with opposite spin. Our model implies that gravitons carry ±1 and 0 fundamental units of charge. The model also suggests a net emmission on order of $E_P/(2r_s)$ from black holes, in addition to Hawking radition, before the background temperature of these standing gravity waves is considered. Our vacuum solutions imply electric and magnetic scalar quadrupoles, of anti-aligned spin 2 gravitons. Such charged gravitons could be produced as pairs of from four or more coincident, spin-aligned photons of any energy, such as could be produced via stimulated emission, though detection might require careful tuning and background subtraction. Barring the existence of charged gravitons, our treatment of the Schwarzschild metric still implies gravitational mass monopole coupling. The existence of gravitational monopole interaction solutions, to order-of-magnitude, could explain dark energy, while being compatible with current astrophysical observations, without admitting a tunable parameter that isn't self-consistently fixed. These particles could act as an inflaton. The zero kinetic energy, zero separation limit of hypothetical charged gravitons could give us a mechanism whereby charge arises from vacuum without infinite self energy, as well as set the absolute zero energy gauge of gravity. This points toward a unification of gravity with the other fundamental forces. The quantization procedure, decomposition in basis states, and mechanical behavior, for these vacuum systems of real gravitons, is obvious nearly to the point of triviality. The mere existence of solutions for entangled, anti-spin-aligned graviton states, with the full spectrum of graviton states carrying interactions in every conserved quantity, offers tremendous economy of theory, in agreement with existing observational data, without "new physics."

References

[1] Benjamin P Abbott, Richard Abbott, TD Abbott, MR Abernathy, Fausto Acernese, Kendall Ackley, Carl Adams, Thomas Adams, Paolo Addesso, RX Adhikari, et al. Observation of gravitational waves from a binary black hole merger. *Physical Review Letters*, 116(6):061102, 2016.

[2] PAR Ade, N Aghanim, M Arnaud, M Ashdown, J Aumont, C Baccigalupi, AJ Banday, RB Barreiro, N Bartolo, E Battaner, et al. Planck 2015 results-xiv. dark energy and modified gravity. *Astronomy & Astrophysics*, 594:A14, 2016.

[3] Ch Alcock, RA Allsman, D Alves, R Ansari, E Aubourg, TS Axelrod, P Bareyre, J-Ph Beaulieu, AC Becker, DP Bennett, et al. Eros and macho combined limits on planetary-mass dark matter in the galactic halo. *The Astrophysical Journal Letters*, 499(1):L9, 1998.

[4] Miguel Alcubierre. The warp drive: hyper-fast travel within general relativity. *Classical and Quantum Gravity*, 11(5):L73, 1994.

[5] Richard Arnowitt, Stanley Deser, and Charles W Misner. Republication of: The dynamics of general relativity. *General Relativity and Gravitation*, 40(9):1997–2027, 2008.

[6] Abhay Ashtekar and Martin Bojowald. Quantum geometry and the Schwarzschild singularity. *Classical and Quantum Gravity*, 23(2):391, 2005.

[7] Anna Barnacka, J-F Glicenstein, and R Moderski. New constraints on primordial black holes abundance from femtolensing of gamma-ray bursts. *Physical Review D*, 86(4):043001, 2012.

[8] Jacob D Bekenstein. Black-hole thermodynamics. *Physics Today*, 33(1):24–31, 1980.

[9] Carl Brans and Robert H Dicke. Mach's principle and a relativistic theory of gravitation. *Physical Review*, 124(3):925, 1961.

[10] Fabio Capela, Maxim Pshirkov, and Peter Tinyakov. Constraints on primordial black holes as dark matter candidates from capture by neutron stars. *Physical Review D*, 87(12):123524, 2013.

[11] S Carlip. Aberration and the speed of gravity. *Physics Letters A*, 267(2):81–87, 2000.

[12] Sean M Carroll. *Spacetime and geometry. An introduction to general relativity*, volume 1. 2004. p.193.

[13] Serguei Chatrchyan, Vardan Khachatryan, Albert M Sirunyan, Armen Tumasyan, Wolfgang Adam, Ernest Aguilo, T Bergauer, M Dragicevic, J Erö, C Fabjan, et al. Observation of a new boson at a mass of 125 Gev with the CMS experiment at the LHC. *Physics Letters B*, 716(1):30–61, 2012.

[14] YM Cho. Theory of gravitational monopole. Technical report, 1990.

[15] Paul AM Dirac. The theory of gravitation in Hamiltonian form. In *Proceedings of the Royal Society of London A: Mathematical, Physical and Engineering Sciences*, volume 246, pages 333–343. The Royal Society, 1958.

[16] François Englert and Robert Brout. Broken symmetry and the mass of gauge vector mesons. *Physical Review Letters*, 13(9):321, 1964.

[17] Richard P. Feynman. *Feynman Lectures on Gravitation.* Addison-Wesley Publishing, 1995.

[18] Yaakov Friedman and Tzvi Scarr. Uniform acceleration in general relativity. *General Relativity and Gravitation*, 47(10):121, 2015.

[19] Gerald S Guralnik, Carl R Hagen, and Thomas WB Kibble. Global conservation laws and massless particles. *Physical Review Letters*, 13(20):585, 1964.

[20] Stephen W Hawking. The path-integral approach to quantum gravity. In *General relativity.* 1979.

[21] M Headrick. A Mathematica package for tensor algebra and calculus. http://goo.gl/UDso5q, 2013. Accessed: 2015-12-16.

[22] Peter W Higgs. Broken symmetries and the masses of gauge bosons. *Physical Review Letters*, 13(16):508, 1964.

[23] Gerd Kortemeyer, Philip Tan, and Steven Schirra. A slower speed of light: Developing intuition about special relativity with games. In *FDG*, pages 400–402, 2013.

[24] LD Landau and EM Lifshitz. *The Classical Theory of Fields*. 1951.

[25] Rosario Martin and Enric Verdaguer. Stochastic semiclassical gravity. *Physical Review D*, 60(8):084008, 1999.

[26] DV Martynov, ED Hall, BP Abbott, R Abbott, TD Abbott, C Adams, RX Adhikari, RA Anderson, SB Anderson, K Arai, et al. Sensitivity of the advanced ligo detectors at the beginning of gravitational wave astronomy. *Physical Review D*, 93(11):112004, 2016.

[27] P O Mazur. Proof of uniqueness of the Kerr-Newman black hole solution. *Journal of Physics A: Mathematical and General*, 15(10):3173, 1982.

[28] Michael P Muno and Jon Mauerhan. Mid-infrared emission from dust around quiescent low-mass x-ray binaries. *The Astrophysical Journal Letters*, 648(2):L135, 2006.

[29] T Padmanabhan. Holographic gravity and the surface term in the Einstein-Hilbert action. *Brazilian Journal of Physics*, 35(2A):362–372, 2005.

[30] T Padmanabhan. A short note on the boundary term for the Hilbert action. *Modern Physics Letters A*, 29(08):1450037, 2014.

[31] Roger Penrose. The question of cosmic censorship. *Journal of Astrophysics and Astronomy*, 20(3):233–248, 1999.

[32] Roger Penrose and RM Floyd. Extraction of rotational energy from a black hole. *Nature*, 229(6):177–179, 1971.

[33] W Rindler. Hyperbolic motion in curved space time. *Physical Review*, 119(6):2082, 1960.

[34] Carlo Rovelli. Loop quantum gravity. *Living Rev. Rel*, 1(1):41–135, 1998.

[35] Jun John Sakurai and Jim Napolitano. *Modern Quantum Mechanics*. Addison-Wesley, second edition, 2011.

[36] Peter Schmitt. Personal communication, July 2017.

[37] Patrick Tisserand, L Le Guillou, C Afonso, JN Albert, J Andersen, R Ansari, É Aubourg, P Bareyre, JP Beaulieu, X Charlot, et al. Limits on the macho content of the galactic halo from the eros-2 survey of the magellanic clouds. *Astronomy & Astrophysics*, 469(2):387–404, 2007.

[38] Edward P Tryon. Is the universe a vacuum fluctuation? *Nature*, 246(5433):396, 1973.

[39] Clifford M Will. The confrontation between general relativity and experiment. *Living Reviews in Relativity*, 17(1):4, 2014.

[40] G ZHAN and GJ WAN. Review of supersymmetry. *Journal of Shaanxi Normal University (Natural Science Edition)*, 14(3), 2000.